Name: _____

CIS 351 Sample Quizzes

Quiz 1

NR1: Binary

Note: To receive credit, you *must* show your work.

(a) Convert 50 from decimal to binary:

(b) Convert 101011 from binary to decimal:

(c) What is the range of integers that can be represented using 7 bits?

(d) How many bits are needed to store integers up to (*and including*) 47?

(e) Write the next six successive binary numbers by using the binary counting pattern. Do *not* convert to decimal or any other number base. Add notes to the right documenting your thought process. (You need only enough notes to convince me that you didn't just convert to base 10 on a scratch sheet of paper.)
110101
_____
_____
_____
_____
_____
_____

Name: _____

NR3: Hexadecimal

When converting, go *directly* between binary and hexadecimal. Do *not* convert to decimal

(a) Convert `43ca` from hexadecimal to binary:

(b) Convert `111101011010010` from binary to hexadecimal:

(c) Write the six successive hexadecimal numbers by following the hexadecimal counting pattern. Do *not* convert to decimal or any other number base. Add notes to the right documenting your thought process. (You need only enough notes to convince me that you didn't just convert to base 10 on a scratch sheet of paper.)
`0x5b98`

_____
_____
_____
_____
_____
_____

NR4: Other Number Bases

Note: To receive credit, you *must* show your work.

(a) Convert 2011_3 from base 3 to decimal:

(b) Convert 172 from decimal to base 4:

Name: _____

CL1: Truth Tables

Construct a truth table that shows the output of a circuit that takes a four-bit integer as input and returns `true` if the input is a multiple of 5.

A	B	C	D	
0	0	0	0	
0	0	0	1	
0	0	1	0	
0	0	1	1	
0	1	0	0	
0	1	0	1	
0	1	1	0	
0	1	1	1	
1	0	0	0	
1	0	0	1	
1	0	1	0	
1	0	1	1	
1	1	0	0	
1	1	0	1	
1	1	1	0	
1	1	1	1	

Name: _____

CL2: Boolean Expressions

(a) Complete the truth table below so that it describes the output of this Boolean expression: $xy + \bar{z}$.

X	Y	Z	$xy + \bar{z}$
0	0	0	
0	0	1	
0	1	0	
0	1	1	
1	0	0	
1	0	1	
1	1	0	
1	1	1	

(b) Write a Boolean expression in sum-of-product form that describes the following truth table:

X	Y	Z	
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1

CL3: Circuit Representation

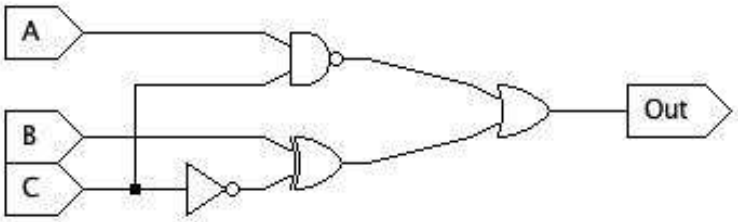
(a) Draw a circuit that implements the truth table below:

A	B	C	Out
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	0

Name: _____

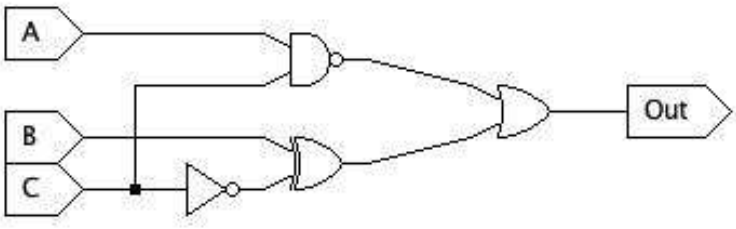
(b) Complete the truth table below to show the output of the circuit for each input:

A	B	C	Out
0	0	0	
0	0	1	
0	1	0	
0	1	1	
1	0	0	
1	0	1	
1	1	0	
1	1	1	



(c) Draw a combinatorial circuit that implements this Boolean expression: $\overline{(AC)} + (B \oplus \bar{C})$

(d) Write the Boolean expression that implements the following circuit:

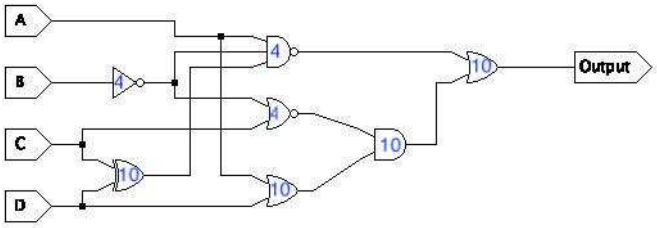


Name: _____

Quiz 2

CL4: Propagation Delay

Compute the propagation delay of the circuit below given the individual gate delays:



ADD1: Binary Addition

Add 11001100 + 01010101 *directly* in binary (i.e., do not convert to decimal first). Show your work so it is clear that you performed the addition in binary.

```
  11001100
+ 01010101
----------
```

ADD2: Ripple Carry Adder

(a) Sketch a full adder.

(b) Sketch an 8-bit ripple carry adder. You may treat full adders as "black boxes".

(c) Consider an 8-bit ripple carry adder with a broken wire between C_{out_3} and C_{in_4}. This wire is "stuck at 0" (i.e., always presents as logical false to C_{in_4}). Assume input A is 10111000. Describe the set of values for B that will result in correct output in spite of the broken wire.

Name: _____

FC1: Functional Completeness

Write a formal proof that the set {NOT, AND} is logically complete.

Name: _____

Quiz3

NR2: Two's Complement

To receive credit, you *must* show your work.

(a) Convert -42 from decimal to and *eight-bit* two's complement number:

(b) Convert 11010100 from two's complement to decimal:

(c) What is the range of integers that can be represented using 8 two's complement bits?

(d) How many bits are needed to store integers between -76 and 37 (*inclusive*) using two's complement?

(e) Write the six *successive* two's complement numbers by using the pattern. Do *not* convert to decimal or any other number base. Add notes to the right documenting your thought process. (You need only enough notes to convince me that you didn't just convert to base 10 on a scratch sheet of paper.)
11100001
_____
_____
_____
_____
_____
_____

Name: _____

ADD3: Carry Lookahead Adder

(a) Sketch the lookahead logic for the carry into column 4. (Columns are indexed beginning with 0.)

(b) Suppose one were to make a mistake and accidentally use an `AND` gate in place of the rightmost `OR` gate for the carry lookahead logic. Describe the inputs A and B that would produce a value of 1 on the carry out.

Name: _____

ADD4: Carry Select Adder

(a) Sketch the top-level of a 16-bit carry-select adder.

(b) Assume that the carry-select pattern is applied at only the top-level, and that the component 8-bit adders are standard ripple-carry adders. Fill in the blanks: The propagation delay of this carry select adder is _____ (more than, exactly, less than) _____ (give a fraction) that of a 16-bit ripple carry adder.

(c) Explain your choice of "more than", "exactly", or "less than" for the previous problem.

Name: _____

ADD5: Recognize Overflow

Given an 4-bit adder, complete the table below to show the carry out and overflow for each pair of inputs.

A		B		C_{out}	Overflow
0	(0000)	0	(0000)		
-1	(1111)	-1	(1111)		
5	(0101)	6	(0110)		

Name: _____

Quiz4

BA1: Boolean Algebra

(a) Use Boolean algebra to show that $(B + \overline{C} + \overline{A}B)(BC + A\overline{B} + AC) \iff BC + A\bar{B}\bar{C}$.

(b) Apply DeMorgan's law to $\overline{A + B + C(\bar{A} + D)}$ until only single terms are negated. (In other words, you answer may contain $\bar{A}$, but not $\overline{AB}$ or $\overline{A + B}$.)

CL5: Combinatorial Logic Design

Design a circuit that takes two integers as input and returns the larger integer as output. Assume you have a "less than" circuit. You may draw the `less_than` circuit, muxes, decoders, equality circuits, adders, etc. as "black boxes".

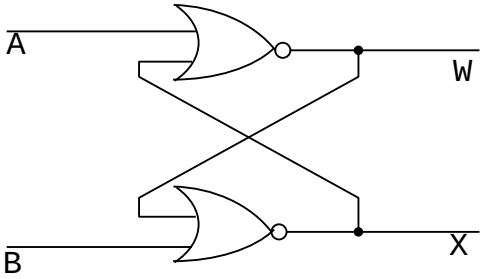
Name: _____

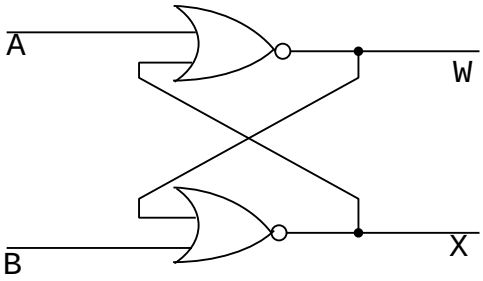
Quiz5

SL1: Latches

(a) Complete the characteristic table for the circuit shown below: Note, there is no clock pulse here. Your answers should show the states W and X after they have reached a steady state given A, B, and current value of W. (Remember to trace the circuit until it has reached a *steady state* — a state in which no further transitions will occur.)

A	B	W_{now}	X_{now}	W_{next}	X_{next}
0	0	0	0		
0	0	0	1		
0	0	1	0		
0	0	1	1		
0	1	0	0		
0	1	0	1		
0	1	1	0		
0	1	1	1		
1	0	0	0		
1	0	0	1		
1	0	1	0		
1	0	1	1		
1	1	0	0		
1	1	0	1		
1	1	1	0		
1	1	1	1		





(Extra copy if you need more scratch space.) NOR latch

(b) The above circuit can be used as a latch (provided you avoid the inputs that lead to random state). What input combinations can be used for "set", "reset", and "hold"? (Hint #1: One or both of the inputs may be "active low". Hint #2: Don't assume that W and X should necessarily hold opposite values — that's why they aren't labeled W and $\bar{W}$.)

(c) Explain how the circuit uses a feedback loop to "remember" the current state. Your explaination should, in part, trace the operation of the "hold" input.

(d) Construct a clocked D latch from the circuit above. Remember, the clocked D latch should set its state to the value of the D input whenever the clock is 1, and hold steady when the clock is 0.

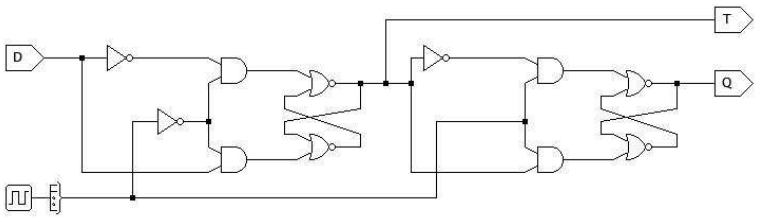
Name: _____

Quiz 6

SL2: Flip-Flops

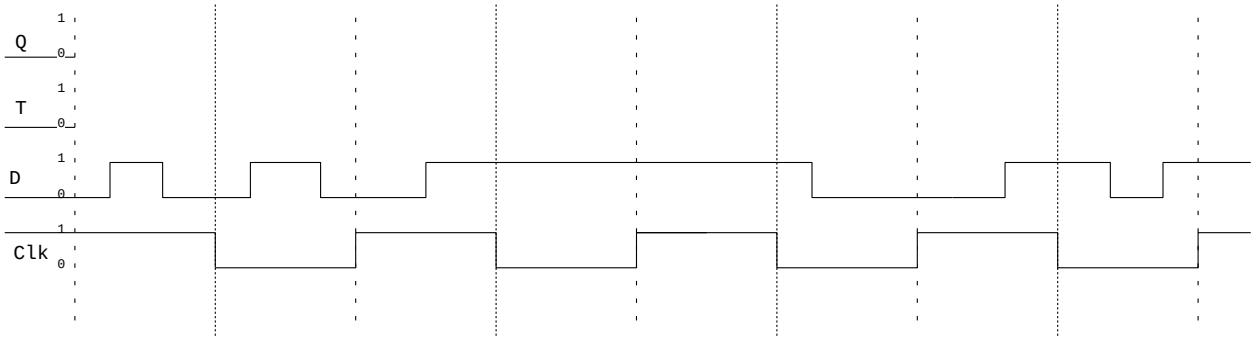
Consider the master-slave flip-flop shown to the right:

(a) Is this a rising-edge, or falling-edge flip-flop? How can you tell?

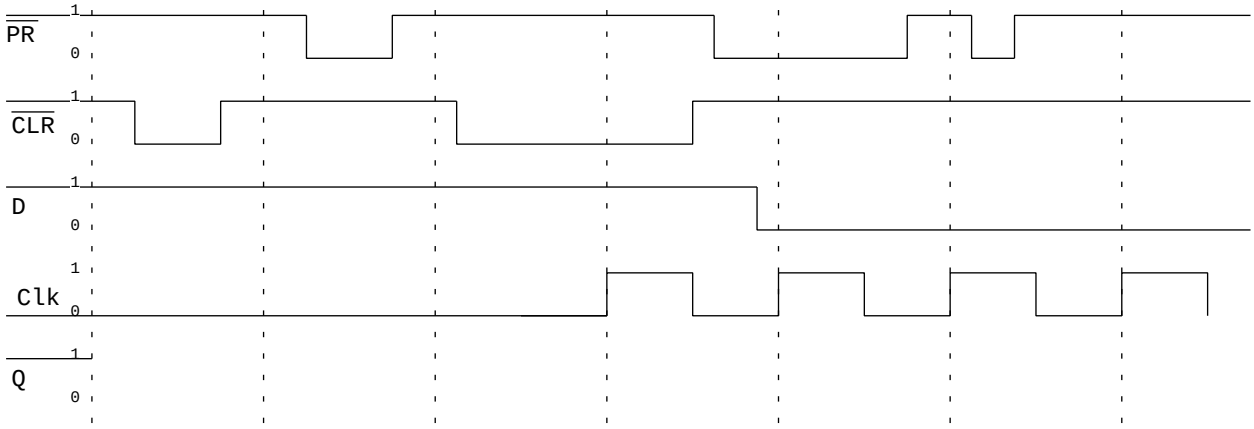


(b) Explain what gives this circuit its "instant trigger point."

(c) Complete the timing diagram below that shows the *internal* operation of the master-slave flip-flop.



(d) Complete the timing diagram below that shows the *external* behavior of the master-slave flip-flop. (This is similar to problems 6-8 on the Sequential Circuit lab.)



Name: _____

SL4: Tracing Sequential Circuits

(a) Complete the characteristic table for the circuit shown below.

Current state			Next State	
B	A_0	A_1	A_0	A_1
0	0	0		
0	0	1		
0	1	0		
0	1	1		
1	0	0		
1	0	1		
1	1	0		
1	1	1		

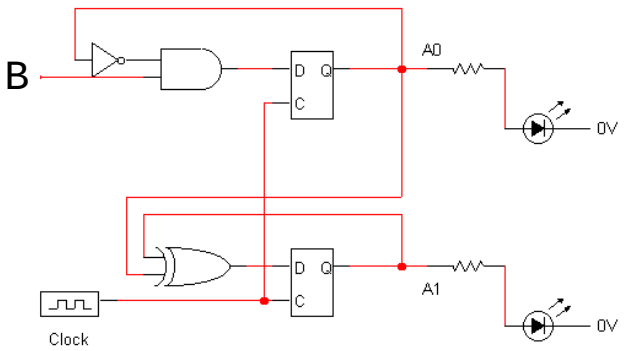
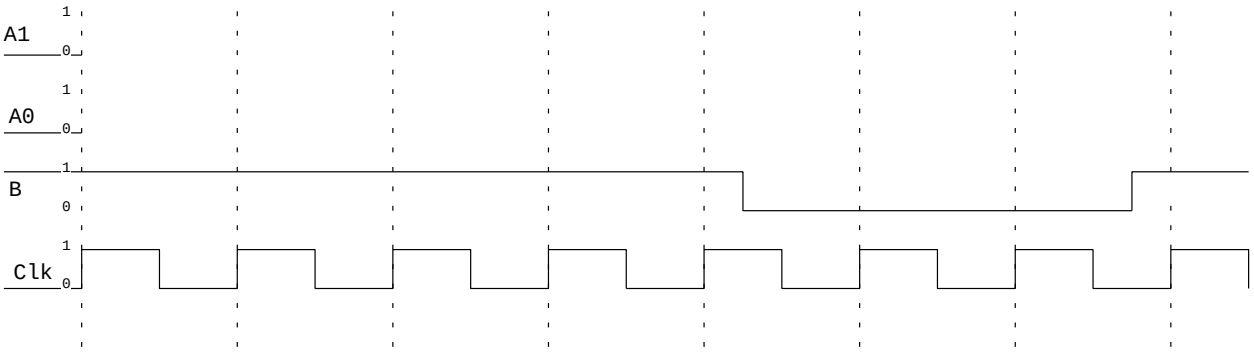


Figure 3-4

(b) Now complete the following timing diagram. Again, remember that the flip-flops are positive-edge triggered. This means that A_0 *and* A_1 *will change* **only** *when the clock rises from 0 to 1!*



Name: _____

Quiz 7

SL6: Design a Sequential Circuit

Design a sequential circuit that will examine a sequence of characters and determine whether all five vowels are present in the string. The circuit will have one 8-bit input that will contain the ASCII representation of a character. On each clock tick, the input will contain the next character in the sequence. The circuit also has a 1-bit output that is initially `false` and becomes `true` once all five vowels have been observed. You may treat sub-circuits "`is a`", "`is e`", "`is i`", "`is o`", and "`is u`" as "black boxes".

Name: _____

AL1: Basic Assembly

(a) Convert the following line of Java code to assembly: `t0 = t1 + t2 + t3 - t4 + t5`

(b) Convert the following line of Java code to assembly: `t0 = (t1 ^ t2) & (t3 | !t4)`

(c) Convert the following Java code to assembly. Your answer *must* use `slt` and either `beq` or `bne`. Do not use any pseudoinstructions. Note: This is not a function; it is simply a section of code. Set your code up as if there are more instructions following the block of code (i.e., don't use `jr $ra`).

```
if (t1 - 6 < t2) {
  t0 = t1;
} else {
   t0 = t2 + 4;
}
t1 = t1 + 7
```

(d) Convert the following Java code to assembly:

```
t1 = 0;
for (int t0 = a0; t0 >= 0; t0-= a1) {
  t1 += t0;
}
return t1;
```

Name: _____

Quiz 8

AL3: Read Assembly

Describe in common English what the following functions do.

(a)
```
mysteryFunction1:
slt $t0, $a0, $a1
slt $t1, $a1, $a2
and $v0, $t0, $t1
jr $ra
```

(b) Describe in common English what the following function does. Hint: It takes two integer parameters. `sra` stands for "shift right arithmetic". It moves all the bits in the register to the right the specified amount.

```
mysteryFunction2:
add $v0, $a0, $a1
sra $v0, $v0, 1
jr $ra
```

Name: _____

Quiz 9

AL2: Intermediate Assembly

Make each element in an array even by subtracting 1 from each odd value. Assume `a0` contains the address of the array and that the array is terminated by the sentinel value -999.

Name: _____

Quiz 10

SS3: Operation of Single Cycle CPU

Answer the questions below with respect to Figure 1.

(a) For each instruction below, list the value on the `RegDest` control wire. *Explain your reasoning.* (The explanation is the important part. Convince me you did more than memorize the table.) Use "X" for "Don't Care" where appropriate.

add	addi	lw	sw	beq	j

(b) What is the purpose of the value on wire `G`? Describe the information it contains when executing a `lw` instruction. (To be clear, I'm looking for the *purpose* of the information, not the specific value.). "This value is not used for this instruction" a valid choice.

(c) What is the purpose of the value on wire `J`? Describe the information it contains when executing a `j` instruction. (To be clear, I'm looking for the *purpose* of the information, not the specific value.). "This value is not used for this instruction" a valid choice.

Name: _____

(d) What is the width (in bits) of the wire labeled `J`? Explain your reasoning / how you know this.

(e) Suppose wire `I` breaks and provides unreliable values. Which of the follwing instructions will continue to function correctly? Explain your reasoning. `add`, `addi`, `lw`, `sw`, `beq`, `j`

(f) Suppose component `R` breaks and provides unreliable values. Which of the follwing instructions will continue to function correctly? Explain your reasoning. `add`, `addi`, `lw`, `sw`, `beq`, `j`

Name: _____

SS5: Single Cycle Design

It would be difficult to add a `swap_register` instruction to the MIPS CPU (i.e, an instruction that takes two registers and swaps their contents). What would be the main difficulty in adding this instruction?

SS5: Single Cycle Design

Consider the instruction `sw R1, offset(R2)`. The CPU in the book implements this instruction by placing `R1` in the "`rt`" position (bits 16-20 in the instruction) and placing `R2` ini the "`rs`" position (bits 21-25) in the instruction.

Would it work equally well to swap the position of these two paramters (i.e., put `R1` on bits 21-25 and put `R2` on bits 16-20)? If so, explain why. If not, explain why not.

Name: _____

Quiz 11

SS4: Modify the Single-Cycle CPU

Consider this following code:

```
for(int x = 0; x < 1000; x++) {
  array[x] = x*x;
}
```

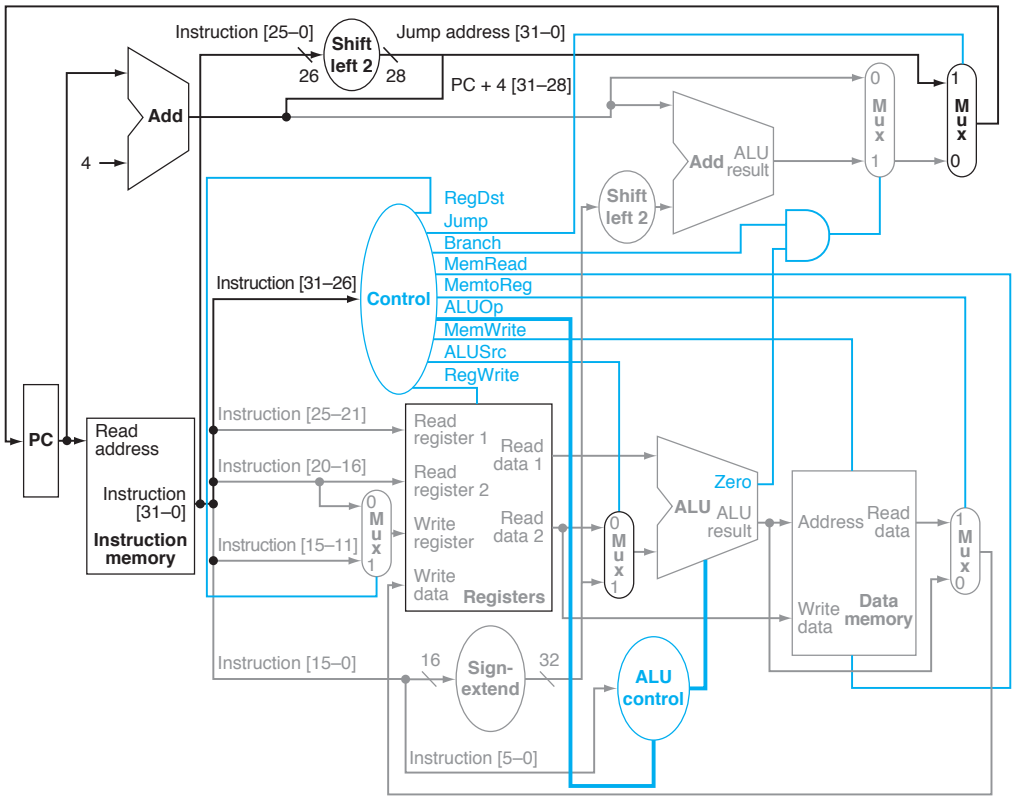
We could save one cycle per loop by combining the storing of data into `array` with the increment of `x` into a new instruction *store word and increment* (`swi R1, R2, increment`). This new instruction will do the following in a single cycle: (1) store the contents of R1 into the memory location contained in R2, and (2) add `increment` to R2 and store the result back in R2. In other words, the instruction does this: `M[R2] = R1; R2 += increment`.

1. Design this instruction. Specify how each bit if the instruction is used. For example, specify which bits contain R1, which contain R2, and which contain the `increment`.

2. Make any necessary changes to the CPU to support this new instruction. You may add additional muxes and control wires if necessary.

3. Specify how each control wire is set for this instruction (including any new control wires you added).

Name: _____


Instruction [25–0]
Shift left 2
Jump address [31–0]
26
28
PC + 4 [31–28]
Add
4
Add
ALU result
Shift left 2
M u x
RegDst
Jump
Branch
MemRead
MemtoReg
ALUOp
MemWrite
ALUSrc
RegWrite
Instruction [31–26]
Control
PC
Read address
Instruction [31–0]
Instruction memory
Instruction [25–21]
Instruction [20–16]
Instruction [15–11]
Instruction [15–0]
Instruction [5–0]
Read register 1
Read register 2
Write register
Write data
Read data 1
Read data 2
Registers
16
Sign-extend
32
ALU
Zero
ALU result
ALU control
Address
Read data
Write data
Data memory

Name: _____

SS4: Modify the Single-Cycle CPU

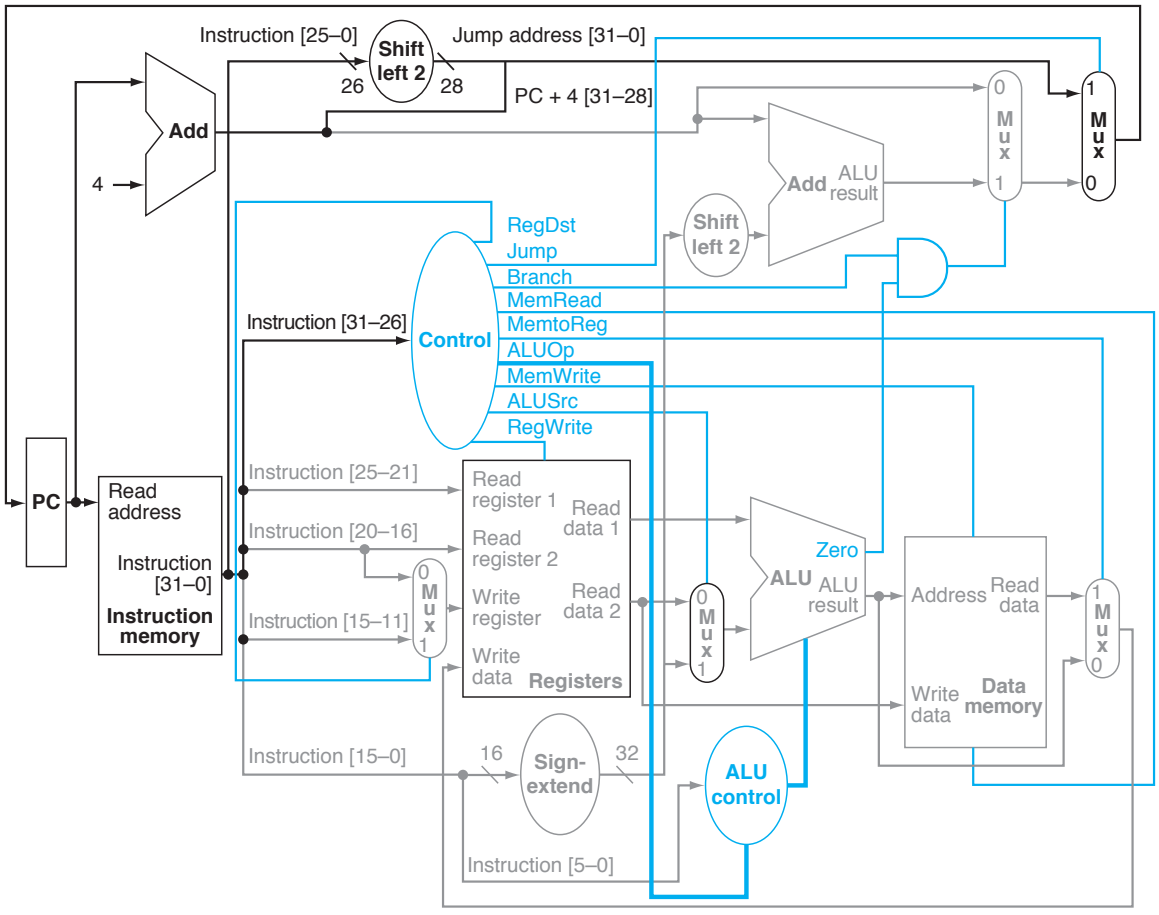
Consider the following `for` statement: `for (rs = 999; rs > 0; rs-= rt)`.

Compiling this code for the single-cycle computer presented in class normally requires at least two instructions: a subtract and a branch. However, it is possible to combine these two operations into a single "decrement and branch if zero" instruction. In particular `dabz $rs, $rt, target` will (1) compute `$rs - $rt`, (2) use that result to decide whether to branch, then (3) write the result back into `$rs`. Register `$rs` is always updated, regardless of whether the branch is taken.

1. Design this instruction. Specify how each bit if the instruction is used. For example, specify which bits contain `rs`, which contain `rt`, and which contain the branch target.

2. Make any necessary changes to the CPU to support this new instruction. You may add additional muxes and control wires if necessary.

3. Specify how each control wire is set for this instruction (including any new control wires you added).



Name: _____

M2: Cache Mechanics

Consider a 512KB, 8-way set associative cache with 16 byte blocks.

(a) Show how 32-bit addresses are divided into offset, index, and tag fields. You must show your work.

(b) Compute the total size of this cache (including metadata). Assume pseudo-LRU replacement. Give your answer in bytes. Show your work.

(c) Sketch this cache.

Name: _____

M3: Trace Cache Behavior

You have an 128KB, byte addressable, 2-way set associative cache with 16 byte blocks. This cache uses an LRU replacement policy. For the following sequence of addresses, show whether each is a hit or a miss. For each cache miss, tell which bytes were replaced.

Address	Tag	Index	H / M	Tags Replaced	Notes
0x12341110					Cold
0x12341113					Same block
0x12351113					Cold
0x12341113					
0x12361114					
0x12351113					
0x12361114					
0x12341110					
0x12361110					Same block
0x12351113					

Name: _____

M4: Effects of Cache Parameters

(a) Suppose you have a cache configured such that the memory address is broken down into t tag bits, i index bits, and o offset bits. If you were to double the cache size without changing the block size or associativity, how would t, i, and o change?

(b) Explain your reasoning for each parameter above (index, offset, and tag).

(c) How does increasing the cache size affect the number of Cold cache misses? Explain your reasoning.

(d) How does increasing the cache size affect the number of Conflict misses? Explain your reasoning.

Name: _____

P1: Pipeline Structure and Speedup

Problem for sample/practice test Consider the following process for baking cookies:

1. Mix sugar, flour, and water using a mixer for six minutes.
2. Pour the mixture into another bowl and add chocolate chips. Stir by hand for four minutes.
3. Spoon the cookie dough onto a baking pan (about four minutes).
4. Place the pan in the oven for fifteen minutes. One pan of cookies takes up the entire oven – you cannot have more than one pan in the oven at once.
5. Place the cookies on a cooling rack (about three minutes). (Assume you have unlimited space on the cooling rack.)

(a) Estimate the total time to bake a single batch of cookies (from when you begin mixing the sugar, flour, and water until all the cookies from the batch are on a cooling rack.)

(b) Suppose you want to pipeline the cookie-baking process, but are working alone. How many stages does your pipeline have? What steps are included in each stage?

(c) What is the primary limitation (i.e., structural hazard) that prevents you from adding a third stage?

(d) Estimate (i) the total time to bake 10 batches of cookies and (ii) the average time per batch.

(e) Your per-batch time is less than the time to make a single batch of cookies. What is the *primary* source of this time savings. (Be specific. Don't just say "pipelining".)

(f) Suppose your pipeline has k stages. The average time per batch is more than $\frac{1}{k}$ the time for a non-pipelined batch. Explain the primary factor that contributes to this less-than-optimal speedup.

Name: _____

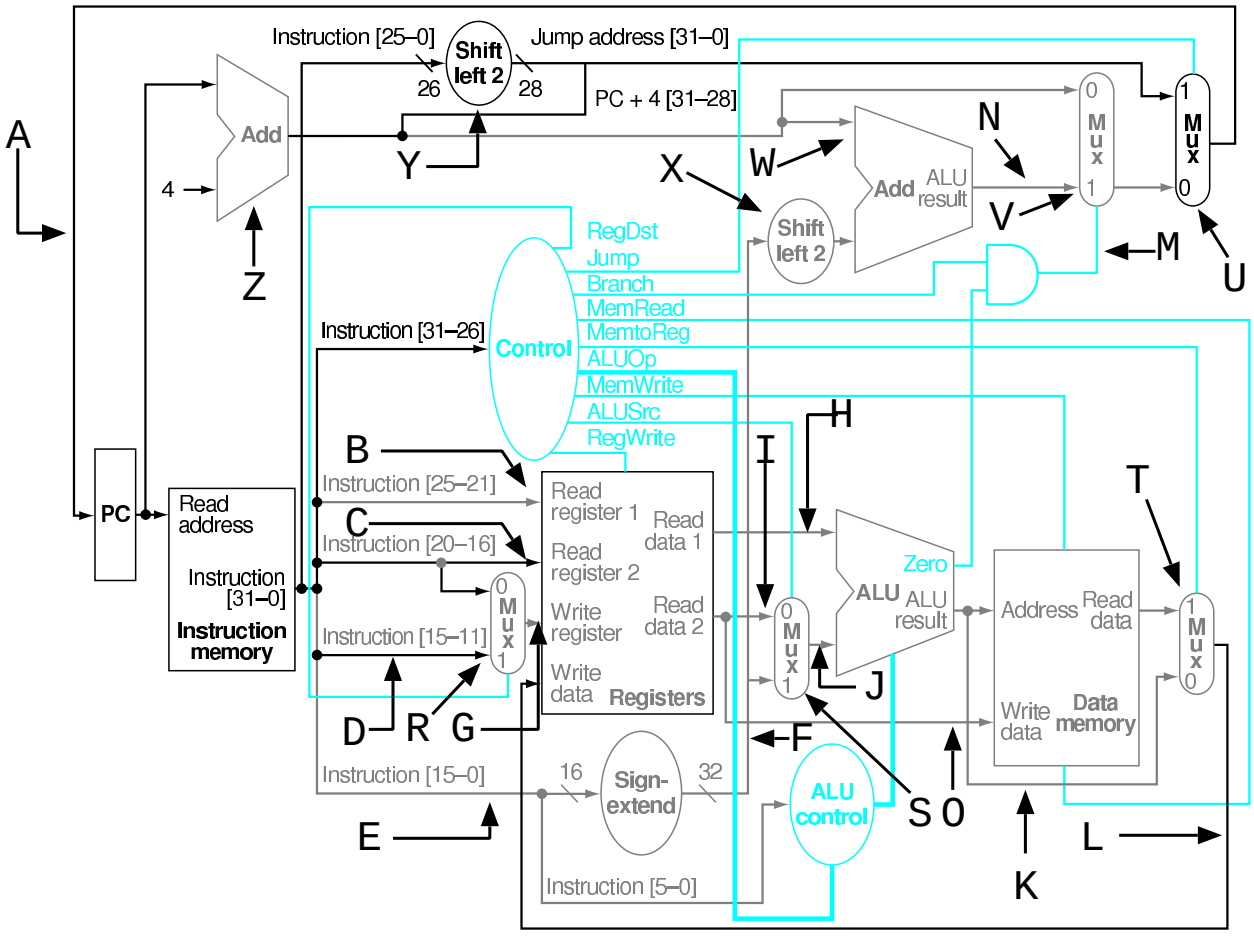


Figure 1: Single Cycle CPU with labeled points